Semester: V						
MATHEMATICS FOR MACHINE LEARNING (Theory) (Group B: Global Elective)						
Course Code	**:**	18G5B17		**CIE**	**:**	**100 Marks**
Credits: L:T:P	**:**	3:0:0		**SEE**	**:**	**100 Marks**
Total Hours	**:**	39L		**SEE Duration**	**:**	**3.00 Hours**

Course Learning Objectives: The students will be able to

1	Understand the basic knowledge on the fundamental concepts of linear algebra that form the foundation of machine intelligence.
2	Acquire practical knowledge of vector calculus and optimization to understand the machine learning algorithms or techniques.
3	Use the concepts of probability and distributions to analyze possible applications of machine learning.
4	Apply the concepts of regression and estimation to solve problems of machine learning.
5	Analyze the appropriate mathematical techniques for classification and optimization of decision problems.

Unit-I	07 Hrs
Linear Algebra: Review of Vector Spaces-Linear Independence, Basis, Rank and Linear Mappings. Affine Spaces, Inner Products, Lengths and Distances, Angles and Orthogonality, Orthonormal Basis, Orthogonal Complement, Inner Product of Functions, Orthogonal Projections, Rotations, Singular Value Decomposition.	
Unit – II	**07 Hrs**
Vector Calculus and Continuous Optimization: Gradients of Vector-Valued Functions, Gradients of Matrices, Identities for Computing Gradients, Backpropagation and Automatic Differentiation, Linearization and Multivariate Taylor Series, Optimization Using Gradient Descent, Constrained Optimization and Lagrange Multipliers and Convex Optimization.	
Unit –III	**08 Hrs**
Probability and Distributions: Construction of a Probability Space, Discrete and Continuous Probabilities, Sum Rule, Product Rule and Bayes' Theorem, Gaussian Distribution, Conjugacy and the Exponential Family, Change of Variables - Inverse Transform.	
Unit –IV	**08 Hrs**
Linear Regression: Problem Formulation, Parameter Estimation, Bayesian Linear Regression, Maximum Likelihood as Orthogonal Projection. **Density Estimation with Gaussian Mixture Models:** Gaussian Mixture Model, Parameter Learning via Maximum Likelihood, EM Algorithm, Latent-Variable Perspective.	
Unit –V	**09 Hrs**
Dimensionality Reduction with Principal Component Analysis (PCA): Problem Setting, Maximum Variance Perspective, Projection Perspective, Eigenvector Computation and Low-Rank Approximations, PCA in High Dimensions, Key Steps of PCA in Practice, Latent Variable Perspective. **Classification with Support Vector Machines:** Separating Hyperplanes, Primal Support Vector Machine, Dual Support Vector Machine, Kernels, Numerical Solution.	

Course Outcomes: After completing the course, the students will be able to	
CO1:	Explore the fundamental concepts of mathematics involved in machine learning techniques.
CO2:	Orient the basic concepts of mathematics towards machine learning approach.
CO3:	Apply the linear algebra and probability concepts to understand the development of different machine learning techniques.
CO4:	Analyze the mathematics concepts to develop different machine learning models to solve practical problems.

Reference Books	
1	Mathematics for Machine Learning, M. P. Deisenroth, A. A. Faisal and C. S. Ong, 1st Edition, 2020, Cambridge University Press.
2	Linear Algebra and Learning from Data, Gilbert Strang, 1st Edition, 2019, Wellesley Cambridge Press, ISBN: 0692196382, 9780692196380.
3	Introduction to Machine Learning, Ethem Alpaydin, 2nd Edition, 2010, PHI Publication, ISBN-978-81-203-4160-9.
4	The Elements of Statistical Learning, Trevor Hastie, Robert Tibshirani and Jerome Friedman, 2nd Edition, 2009, Springer, ISBN: 978-0-387-84857-0, 978-0-387-84858-7.

Continuous Internal Evaluation (CIE); Theory (100 Marks)
CIE is executed by the way of Tests (T), Quizzes (Q),) and Experiential Learning (EL). Three tests are conducted for 50 marks each and the sum of the marks scored from three tests is reduced to 50. Minimum of three quizzes are conducted and each quiz is evaluated for 10 marks adding up to 30 marks. All quizzes are conducted online. Faculty may adopt innovative methods for conducting quizzes effectively. The number of quizzes may be more than three also. The marks component for experiential learning is 20.
Total CIE is 50 (T) +30 (Q) +20 (EL) = 100 Marks.

Semester End Evaluation (SEE); Theory (100 Marks)
SEE for 100 marks is executed by means of an examination. The Question paper for the course contains two parts, Part – A and Part – B. Part – A consists of objective type questions for 20 marks covering the complete syllabus. Part – B consists of five main questions, one from each unit for 16 marks adding up to 80 marks. Each main question may have sub questions. The question from Units I, IV and V have no internal choice. Units II and III have internal choice in which both questions cover entire unit having same complexity in terms of COs and Bloom’s taxonomy level.

CO-PO Mapping												
CO/PO	**PO1**	**PO2**	**PO3**	**PO4**	**PO5**	**PO6**	**PO7**	**PO8**	**PO9**	**PO10**	**PO11**	**PO12**
CO1	3	2	-	1	-	-	-	-	-	-	-	2
CO2	3	2	1	-	-	-	-	-	-	-	-	2
CO3	2	3	2	2	-	-	-	-	-	-	-	1
CO4	3	3	1	2	1	-	-	-	-	-	-	3

High-3: Medium-2: Low-1